

## DETAILED STRUCTURE OF THE $V_h$ -AMYLOSE–IODINE COMPLEX A LINEAR POLYIODINE CHAIN\*

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### ABSTRACT

The structure of the hydrated amylose–iodine complex has been determined by combined methods of X-ray diffraction and stereochemical packing analysis. The unit cell was identified as orthorhombic with  $a = 13.60 \text{ \AA}$ ,  $b = 23.42 \text{ \AA}$ , and  $c = 8.17 \text{ \AA}$  (fibre repeat) with two amylose chains passing through the unit cell. Iodide was found as an almost linear chain in the centre of the six-fold, left-handed amylose helix. Eight water molecules of hydration per unit cell were located in good hydrogen-bonding positions between the amylose helices.

### INTRODUCTION

The structure of the blue starch–iodine complex has been a topic of considerable discussion<sup>1–14</sup>. The studies by Rundle and co-workers<sup>1–5,6</sup> of various amyloses and amylose complexes led to the proposal that the amylose chains crystallise in a six-fold helical conformation. The proposal<sup>6</sup>, based on X-ray diffraction experiments, that iodine occupies the otherwise open channel in the centre of the amylose helix verified chemical predictions of other workers<sup>12,13</sup>. However, a detailed structural investigation was not possible and, subsequently, the stereochemical disposition of the iodine in the central cavity of the helix was not determined. West<sup>9,10</sup> suggested that the iodide in the amylose–iodine complex, as well as in other polymeric materials, existed as a linear array at equal interatomic distances of  $3.1 \text{ \AA}$ . Other investigators have presented supporting evidence<sup>8,13</sup>. On the other hand, Stein and Rundle<sup>7</sup> developed a theory explaining the interaction of iodide with the amylose helix as a dipole–dipole interaction which predicts non-equivalent I–I separation distances.

Crystallographic studies of model compounds<sup>15,16</sup> of the amylose–iodine complex, such as cyclohexa-amylose complexed with iodine, have been undertaken

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In these studies, the complexed iodine was present as either  $I_2$ ,  $I_3^-$ , or  $I_5^-$  species. However, these model compounds do not exhibit the continuous nature of the amylose helix. In a recent study<sup>27</sup> with the resonance Raman/iodine Mossbauer technique,  $I_5^-$  was detected in the iodine-starch complex.

In view of recent successes in solving polysaccharide structures involving complexation with small molecules<sup>17, 18</sup>, we have reinvestigated the amylose-iodine complex. In this investigation, X-ray diffraction methods were combined with those of stereochemical packing analysis<sup>19</sup>. Debye-Scherrer X-ray intensity data<sup>20</sup>, as well as X-ray data from amylose-iodine fibre diagrams, were used.

## EXPERIMENTAL

V-Amylose-iodine films were prepared by casting films from a 15% (w/w) solution in  $Me_2SO$ . The films were then stretched in high relative humidity at room temperature to an extension of 200–600%. These stretched films, which produced oriented-fibre X-ray diagrams typical of the  $Me_2SO$ -amylose complex<sup>21</sup>, were then placed in boiling methanol for 20 min whilst held under tension, after which they exhibited X-ray diagrams of  $V_h$ -amylose. The films were next placed, still under tension, in a chamber containing iodine vapour at 100% relative humidity for 6 h. After this treatment, the films possessed the intense blue colour characteristic of the amylose-iodine complex and gave the fibre X-ray diagram shown in Fig. 1.

X-Ray diffractograms for  $d$ -spacing measurements were recorded on flat film in an evacuated camera at a film-to-sample distance of 5 cm. For intensity measure-

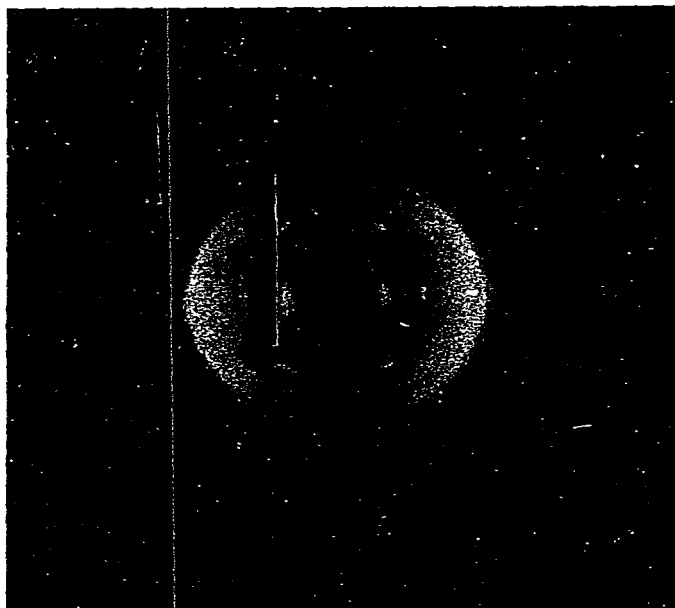


Fig. 1. Fibre diffraction diagram of the  $V_h$ -amylose-iodine complex.

ments, the diffracted X-ray intensities were collected on multiple film packs in an evacuated cylindrical camera of 5.73-cm radius. Ilford Industrial G film was used throughout. The intensities were measured, corrected, and converted into structure amplitudes as previously described<sup>18</sup>. CuK $\alpha$  radiation was used. The structure amplitudes for overlapping reflections were calculated as composites from  $|F_c| = (\sum_i m_i F_{ci}^2)^{1/2}$ , where  $m_i$  is the multiplicity, and the summation is carried out over all diffracting planes contributing to the composite. Unobserved intensities were assigned relative intensity values of one-half of the minimum observable intensity in that region of the scattering angle and weighted one-half in the calculation of a weighted  $R$  value.

The sixteen individual reflections observed on the fibre diagram were sufficient to identify the unit cell as orthorhombic with  $a = 13.60$  Å,  $b = 23.42$  Å, and  $c = 8.17$  Å (fibre repeat). However, these data were insufficient to carry out a detailed refinement of the structure against X-ray data. Therefore, the Debye-Scherrer data collected previously by Zaslow and Miller<sup>20</sup> were used after being indexed with the orthorhombic unit-cell as determined from the fibre X-ray diagram. The Debye-Scherrer data were corrected for Lorentz and polarisation effects and then converted into structure amplitudes. Since only zero- and first-order layer lines were observed on the fibre diagram, only  $hkl$  indices with  $l = 0$  or  $l = 1$  were considered in indexing the Debye-Scherrer intensity envelopes. No separation was attempted between zero and first-order layer lines, i.e.,  $l = 0$  or  $l = 1$ . Relative intensities measured by Zaslow and Miller agreed well with those present on the fibre diagram.

## RESULTS AND DISCUSSION

The dimensions of the V-amylose unit-cell increase with increasing degree of hydration<sup>6</sup>. The anhydrous polymorph (V<sub>a</sub>) exhibits an  $a$  axis of 13.0 Å. In the fully hydrated (V<sub>h</sub>) form, the  $a$  axis is 13.7 Å. Amylose-iodine complexes can also occur in anhydrous and hydrated forms<sup>20</sup>. The structure investigated showed an  $a$  axis of 13.6 Å, indicative of a highly hydrated condition.

The space group of V<sub>a</sub>- and V<sub>h</sub>-amylose was previously determined as P2<sub>1</sub>2<sub>1</sub>2<sub>1</sub> with sections of two chains passing through the unit cell. Since the unit-cell volumes of V<sub>a</sub>-amylose, V<sub>h</sub>-amylose, and the amylose-iodine complex are similar (2304 Å<sup>3</sup> compared to 2604 and 2602 Å<sup>3</sup>, respectively), we assumed that sections of two amylose chains also pass through the amylose-iodine unit-cell. Due to the possibility of having an odd number of iodide atoms in the fibre direction per fibre repeat, the space group P2<sub>1</sub> was chosen as most probable, with the only 2<sub>1</sub> screw-axis perpendicular to the  $a,c$  plane of the unit cell (second setting). This space group, P2<sub>1</sub>, is included in P2<sub>1</sub>2<sub>1</sub>2<sub>1</sub>, but of lower symmetry. Although the distribution of the iodine species (chain) might be at random in the centre of the amylose helix, this space group is nevertheless a good choice for the amylose helix itself and, as will be discussed later, also for the iodine species. Systematic absences of reflections agreed with space group

TABLE I

(a) CARTESIAN CO-ORDINATES (Å) OF THE FIRST RESIDUE OF  $V_h$ -AMYLOSE-IODINE IN THE REFERENCE POSITION<sup>a</sup>

Atom	X	Y	Z	Atom	X	Y	Z
O-4	0 000	-4 131	0 000	O-5	-3 570	-3 520	-0 472
C-1	-3 935	-3 341	0 878	O-6gg	-2 170	-4 827	-2 707
C-2	-3 240	-4 383	1 740	H-1	-4 974	-3 462	0 969
C-3	-1 731	-4 347	1 537	H-2	-3 591	-5 333	1 464
C-4	-1 388	-4 454	0 057	H-3	-1 350	-3 446	1 918
C-5	-2 158	-3 394	-0 725	H-4	-1 575	-5 419	-0 314
C-6	-1 964	-3 496	-2 227	H-5	-1 842	-2 445	-0 408
O-2	-3 586	-4 150	3 104	H-6A	-0 995	-3 179	-2 478
O-3	-1 128	-5 443	2 224	H-6B	-2 655	-2 861	-2 697

(b) CARTESIAN CO-ORDINATES (Å) OF IODINE AND WATER IN ONE ASYMMETRIC UNIT OF SPACE GROUP  $P2_1$ 

I-1	3 696	-0 099	0 016	O-W1	3 125	-8 734	1 004
I-2	3 247	-0 231	2 889	O-W2	-4 548	-5 485	-0 180
I-3	3 311	0 202	5 768	O-W3	3 675	8 734	5 089
				O-W4	-2 262	5 485	3 905

(c) FRACTIONAL ATOMIC CO-ORDINATES FOR ONE RESIDUE OF THE  $6_5$   $V_h$ -AMYLOSE-IODINE COMPLEX CHAIN AND THE WATER AND IODINE MOLECULES OF ONE ASYMMETRIC UNIT IN SPACE GROUP  $P2_1$ . THE VIRTUAL-BOND LENGTH (O-4 O-4<sub>2</sub>) IS 4.35 Å

O-4	0 5381	0 0560	-0 3599	O-5	0 5787	-0 0969	-0 4176
C-1	0 5748	-0 1141	-0 2524	O-6gg	0 6372	-0 0225	-0 6912
C-2	0 6312	-0 0718	-0 1469	H-1	0 6075	-0 1545	-0 2412
C-3	0 5935	-0 0112	-0 1717	H-2	0 7057	-0 0732	-0 1807
C-4	0 5930	0 0041	-0 3529	H-3	0 5218	-0 0080	-0 1251
C-5	0 5370	-0 0414	-0 4486	H-4	0 6646	0 0096	-0 3983
C-6	0 5396	-0 0322	-0 6324	H-5	0 4635	-0 0415	-0 4098
O-2	0 6230	-0 0890	0 0201	H-6A	0 4949	0 0028	-0 6632
O-3	0 6559	0 0281	-0 0876	H-6B	0 5114	-0 0687	-0 6900
<i>Iodine and water</i>							
I-1	0 2718	-0 0042	0 0020	O-W1	0 2298	-0 3729	0 1229
I-2	0 2387	-0 0099	0 3536	O-W2	-0 3337	-0 2342	-0 0220
I-3	0 2435	0 0086	0 7060	O-W3	0 2702	0 3729	0 6229
				O-W4	-0 1663	0 2342	0 4780

<sup>a</sup>For proper positioning in the unit cell, the residue must be shifted 1/4 in  $a$  as is necessary for space group  $P2_1$ , in the second setting, rotated 108.5° around  $z$ , and shifted -2.94 Å along  $z$ . The virtual bond length O-4 O-4<sub>2</sub> is 4.35 Å.

P2<sub>1</sub> The amount of iodine taken up by amylose had previously been estimated as 26% by weight, corresponding to 2.2 iodide atoms per six glucosyl residues

Conformation and packing analysis was performed by the method of stereochemical refinement analysis<sup>19</sup> The left-handed, helical conformation of amylose that had been found in previous studies of V<sub>a</sub>-amylose<sup>22</sup> and V-Me<sub>2</sub>SO-amylose<sup>21</sup> was adjusted to the 8.17-Å helix pitch, as measured for V<sub>h</sub>-amylose-iodine. It was found that the most convenient virtual-bond length O-4—O-4<sub>2</sub> was 4.35 Å, compared to 4.28 Å in V<sub>a</sub>-amylose<sup>19</sup>, for a discussion of virtual-bond terminology, see ref. 24. The glycosidic angle (C-1—O-4<sub>2</sub>—C-4<sub>2</sub>) was 120°, and two intramolecular hydrogen-bonds occur in this conformation: O-2—O-3<sub>2</sub> of adjacent residues with length of 2.98 Å, and O-2—O-6<sub>7</sub> of succeeding turns with 2.83 Å. The most stable rotamer of O-6 was in the vicinity of *gg*\* [ $\tau(\text{O-5-C-5-C-6-O-6}) = 72^\circ$ ]. No non-bonded contacts occur below the cut-off distances<sup>26</sup>. The shortest H—H distances is H-1—H-4<sub>2</sub> at 2.18 Å.

Helices having the conformation described above were packed stereochemically in the unit cell with helix rotations, helix translations, and all bond lengths, bond angles, and torsion angles as the variable parameters<sup>19</sup>. The starting model for

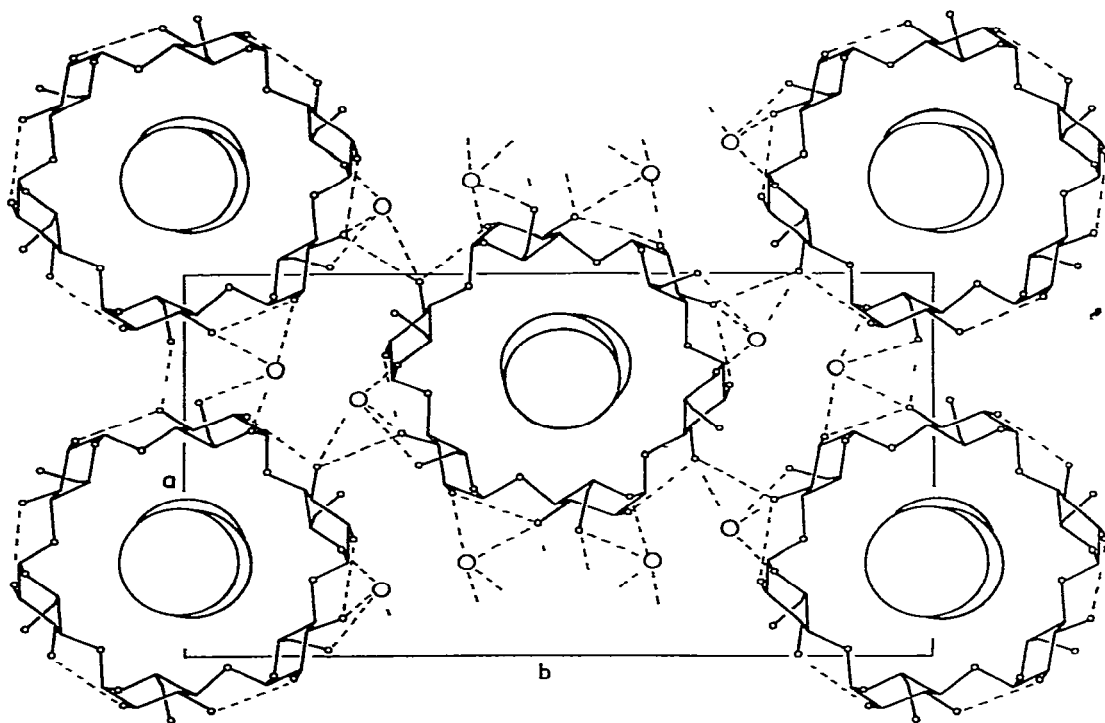


Fig. 2. View of the V<sub>h</sub>-amylose-iodine complex in the *a,b* plane of the unit cell, showing the hydrogen-bonding arrangement.

\**gg* means *gauche* to both O-5 and C-4

TABLE II

POSSIBLE INTRA- AND INTER-MOLECULAR HYDROGEN-BONDS<sup>a</sup> FOR THE V<sub>h</sub>-AMYLOSE-IODINE COMPLEX

Hydrogen bond	Distance (Å)
<i>Intra</i>	
O-2 O-3 <sub>2</sub>	2.98
O-2 O-6 <sup>-</sup>	2.83
<i>Inter</i>	
O-3 <sub>2</sub> O-3 <sub>1</sub> <sup>b</sup>	2.88
O-3 O-6 <sup>c</sup>	2.94
O-5 O-W1 <sup>c</sup>	2.74
O-6 O-W1 <sup>c</sup>	2.81
O-3 O-W1 <sup>c</sup>	2.81
O-2 <sub>3</sub> O-W1 <sup>b</sup>	2.76
O-5 <sub>2</sub> O-W2 <sup>c</sup>	2.63
O-6 <sub>3</sub> O-W2 <sup>c</sup>	2.92
O-3 <sub>3</sub> O-W2 <sup>b</sup>	2.73
O-3 <sub>2</sub> O-W2 <sup>f</sup>	2.68

<sup>a</sup>As the packing refinement for the amylose helices with the associated water molecules has been performed in space group  $P2_12_12_1$  the space group found for V<sub>h</sub>-amylose only those hydrogen bonds are listed which are unique in this space group. Note: O-W3 and O-W4 are symmetry-related to O-W1 and O-W2 respectively. <sup>b</sup> $1/2 + x - 1/2 - y - z$ ; <sup>c</sup> $1/2 - x - 1/2 - y - 1 - z$ ; <sup>d</sup> $3/2 - x - y - 1/2 + z$ ; <sup>e</sup> $1 - x - 1/2 - y - 1/2 - z$ ; <sup>f</sup> $1 - x - y - z$ .

this refinement was that obtained for V<sub>h</sub>-amylose<sup>28</sup> with 8 water molecules in the unit cell, which had been varied to form an optimal hydrogen-bonding scheme with the amylose helices. The result of this analysis showed additional hydrogen bonds between the amylose helices: between O-3 atoms of adjacent, antiparallel helices with a length of 2.88 Å, and O-3...O-6 of the parallel corner chains with 2.94 Å, and with water molecules as shown in Fig. 2 and listed in Table II. It should be noted that these packing calculations were carried out in the space group ( $P2_12_12_1$ ) in which pure V<sub>h</sub>-amylose crystallises. This procedure was chosen to minimise the variables and to save computer time since the few reflections observed are not sufficient to test for space-group symmetry. No real short-contacts were encountered.

Next, the iodine species were located by trial and error. Preliminary calculations were carried out in space group  $P2_1$  second setting. The iodide atoms were placed in all stereochemically possible positions in the unit cell with the best packing positions of the amylose helices. The crystallographic  $R$  value, defined as  $\sum w ||F_o| - |F_c|| / \sum w |F_o|$  was calculated, where  $|F_o|$  and  $|F_c|$  are the observed and calculated structure amplitudes respectively, and  $w$  is a weight factor. The data set of ref. 20 and an isotropic temperature factor of  $B = 5$  [temperature factor =  $\exp(-B \sin^2 \theta)$ ] were used. Scattering factors for carbon, hydrogen, oxygen, and iodide were obtained from the International Tables for X-ray Crystallography<sup>25</sup>. The  $R$  value calculated for

the structure without iodide was  $\sim 0.55$ . Placement of the iodide atoms in the interstitial spaces served only to increase the  $R$  value. However, placement in the central channel of the helix resulted in decreased  $R$  values. A minimum in  $R$  was found with three iodide atoms in one turn of the amylose helix, *i.e.*, six iodide atoms per unit cell, which corresponds to an iodine uptake of 35% by weight, in reasonable agreement with previous estimates<sup>5</sup> of 26%.

This procedure for locating the iodine species can only be regarded as crude, since the fibre pattern of the amylose-iodine complex showed one, rather diffuse, meridional reflection at a  $d$ -spacing of  $2.9 \text{ \AA}$  which is incongruous with the layer-line spacing of  $2.72 \text{ \AA}$  of the amylose helices. Therefore, if the iodine species do contribute to the scattering of the first layer line, a splitting of this layer line is to be expected due to the scattering of the amylose helices and the iodine species, respectively. However, such a splitting was not observed. This experimental evidence can be interpreted as indicating that polyiodide chains having an average spacing of  $2.9 \text{ \AA}$  between the iodide atoms in the  $z$  direction are distributed at random inside the amylose helices. Such a distribution of polyiodide chains without the amylose helices will result in equatorial reflections and a meridional reflection of  $2.9 \text{ \AA}$  only. Discrete spots will not be found on any higher layer lines. Unfortunately, no conclusions can be drawn about the lengths of the polyiodide chains.

Therefore, the strategy in placing the iodide atoms inside the helices was to use the equatorial reflections of the fibre pattern and the appearance of a single  $2.9\text{-\AA}$  meridional reflection as X-ray data for the refinement procedure. Two models have been tested: (a) the iodine chain has a three-fold symmetry or (b) a five-fold symmetry along the  $z$  axis, thus mimicking an  $I_3^-$  or  $I_5^-$  species or a longer polyiodide chain with this symmetry, respectively.

In a first step, the iodide atoms were placed in space group  $P1$  in two independent channels with  $c$  dimensions corresponding to (a)  $3 \times 2.9 \text{ \AA}$  or (b)  $5 \times 2.9 \text{ \AA}$  and their positions were calculated by  $R$ -factor refinement using the observed reflections. The amylose helices were not considered during this refinement. Only the missing and observed meridional reflections have been added, thus forcing the iodide atoms to the desired  $2.9\text{-\AA}$  repeat distance in  $z$ . An extreme anisotropic temperature-factor was used for this calculation. With this procedure, the iodide atoms can be located in three dimensions within the unit cell at places where the channels of the amylose helices were expected. The corresponding  $R$  values for model (a) and (b) were almost equal and no significant difference was detected upon adding the unobserved, equatorial structure amplitudes, indicating no preference for either of the two models. Therefore, model (a) was used in further calculations for reasons of simplicity. A symmetry relationship between the two independent iodine species was detected close to space group  $P2_1$ , second setting, with the  $2_1$  screw-axis perpendicular to the  $a,c$ , plane. Therefore, space group  $P2_1$  was used in further calculations.

Next, the amylose helix with the water molecules was added, as obtained by conformation and packing analysis. A refinement of the iodide positions against the  $R$  factor and a combined refinement against  $R$  and packing was undertaken with the

equatorial reflections in space group  $P2_1$ . No significant difference between the two refinement procedures was found, and a final value of 29% in the weighted  $R$  factor and 28% in  $R2$  was obtained. The weights used were one for observed reflections and one-half for unobserved reflections,  $R2$  is the discrepancy factor for the squared difference in the structure amplitudes  $R2 = \{\sum (|F_o| - |F_c|)^2 / \sum |F_o|^2\}^{1/2}$ . The shortest contacts between iodide and other atoms are hydrogen-iodide contacts of 3.3 Å. A refinement of the co-ordinates of the amylose helix did not seem to be useful, in view of the few data and the uncertainty caused by the strong scattering of the iodine species. Therefore, further tests were undertaken to check the results obtained. Calculating the first layer line with 7 pairs of a total of 12 overlapping, observed and unobserved reflections for the  $V_h$ -amylose helices and the water positions only resulted in weighted values of  $R = 36\%$  and  $R2 = 43\%$ . These high values are due to

TABLE III

OBSERVED AND CALCULATED STRUCTURE AMPLITUDES OF A FIBRE X-RAY DIAGRAM OF  $V_h$ -AMYLOSE-IODINE<sup>a</sup>

h k l	$ F_c $	$ F_o $
1 1 0 0 2 0	28	21
2 0 0 1 3 0	12	14
2 2 0, 0 4 0	28	43
3 1 0, 2 4 0, 1 5 0	78	95
3 3 0, 0 6 0	51	31
<i>Unobserved <math>F_o^2</math> taken as one-half of the observable intensity</i>		
1 0 0	0	0
1 2 0	1	2
2 1 0	2	3
1 4 0	6	3
2 3 0	7	3
3 0 0	0	3
3 2 0	11	6
1 6 0	10	7
2 5 0	7	7
3 4 0	5	7
<i>First layer line</i>		
0 1 1	4	6
1 0 1, 1 1 1, 0 2 1	19	18
2 0 1 1 3 1, 2 1 1	9	18
2 2 1, 0 4 1	12	17
<i>Unobserved</i>		
1 2 1	14	2
0 3 1	4	3
1 4 1	7	4

<sup>a</sup>The zero layer line (equator) was calculated with iodide atoms, and the first layer line without iodide atoms. Normalisation constants are 0.057 for the equator and 0.055 for the first layer line.



a large, calculated (121) reflection. The  $R$  values for the observed reflections only were <30%. When the iodide atoms were added, the  $R$  values increased considerably. Use of the 147 pieces of data from the Debye-Scherrer experiment<sup>20</sup>, where no separation of the zero and first layer line can be obtained, resulted in  $R = 31\%$  and  $R_2 = 31\%$ . The calculated and observed structure amplitudes for the fibre pattern are listed in Table III.

Cartesian co-ordinates of the best-refined glucosyl residue by packing and conformation analysis, the water molecules, and the iodide atoms are given in Table I, and possible hydrogen bonds in Table II. Note that the iodide-chain repeat distance in  $z$  is different from that for the amylose helix. The projection of the unit cell onto the  $a,b$  plane is shown in Fig. 2.

## CONCLUSION

A comparison of the V<sub>a</sub>-amylose structure and the V<sub>h</sub>-amylose-iodine structure is of interest. In V<sub>a</sub>-amylose, the fibre repeat is 0.26 Å shorter than the 8.17-Å repeat of V<sub>h</sub>-amylose-iodine. HO-6 Groups were found at three different rotameric positions,  $gt$ ,  $gg$ , and  $tg$ , in V<sub>a</sub>-amylose<sup>19</sup>, resulting in a true 2<sub>1</sub> screw-axis along the polymer chain. However, the HO-6 rotameric positions in V<sub>h</sub>-amylose-iodine were all  $gg$  and along with the three iodide atoms in one turn of the helix, resulted in the absence of a 2<sub>1</sub> screw-axis in the helix direction. The helix rotational position in V<sub>a</sub>-amylose is 88.6° from the reference position (O-4 at 0,  $-y_0, 0$ ), in V<sub>h</sub>-amylose-iodine, it is 108.5°. The helix translation in V<sub>a</sub>-amylose is  $-3.98$  Å and in V<sub>h</sub>-amylose-iodine it is  $-4.98$  Å, with both helices in equivalent positions and the same space group. Therefore, the transition from V<sub>a</sub>-amylose to V<sub>h</sub>-amylose-iodine occurs with a helix rotation of 20° and a translation of 1 Å. Water molecules are found between the helices in V<sub>h</sub>-amylose-iodine and account for the expansion of the unit cell upon hydration. The water molecules are hydrogen-bonded to the hydroxyl groups on the amylose helices in a dense network forming bridges between the chains.

Iodide is found as a polyiodide chain in the helix channels with nearly equal separation distances between the atoms. The distances are 2.91, 2.91, and 2.99 Å. The length of the iodide chain cannot be determined. The I—I—I angles are all nearly linear.

## ACKNOWLEDGMENTS

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